



- a)  $\frac{1}{2}$   
c)  $\frac{1}{3}$

b)  $\frac{2}{5}$   
d)  $\frac{2}{3}$

6. In triangle ABC, D, E and F are the midpoints of sides BC, CA and AB respectively and  $\frac{AB}{DE} = \frac{BC}{FE} = \frac{CA}{FD}$ , then [1]  
  
a)  $\triangle BCA \sim \triangle FDE$   
c)  $\triangle FDE \sim \triangle ABC$

b)  $\triangle CBA \sim \triangle FDE$   
d)  $\triangle FDE \sim \triangle CAB$

7. The mean of the first 10 composite numbers is [1]  
  
a) 11.2  
c) 112

b) 11.4  
d) 12.2

8. If  $(\tan \theta + \cot \theta) = 5$  then  $(\tan^2 \theta + \cot^2 \theta) = ?$  [1]  
  
a) 23  
c) 24

b) 25  
d) 27

9. In  $\triangle ABC$ , a line XY parallel to BC cuts AB at X and AC at Y. If BY bisects  $\angle XYC$ , then [1]  
  
a)  $BC = CY$   
c)  $BC \neq BY$

b)  $BC = BY$   
d)  $BC \neq CY$

10. The product of two successive integral multiples of 5 is 1050. Then the numbers are [1]  
  
a) 25 and 35  
c) 30 and 35

b) 25 and 30  
d) 35 and 40

11. If two positive integers ‘a’ and ‘b’ are written as  $a = pq^2$  and  $b = p^3q^2$ , where ‘p’ and ‘q’ are prime numbers, then LCM(a, b) = [1]  
  
a) pq  
c)  $p^2q^3$

b)  $p^3q^2$   
d)  $p^2q^2$

12. If mode of a series exceeds its mean by 12, then mode exceeds the median by: [1]  
  
a) 4  
c) 6

b) 8  
d) 10

13. The points A (-4, 0), B(4, 0) and C(0, 3) are the vertices of a [1]  
  
a) isosceles triangle  
b) scalene triangle

- c) equilateral triangle                      d) right triangle
14. If the altitude of the sun is  $60^\circ$ , the height of a tower which casts a shadow of length 90 m is [1]
- a) 60 m                      b)  $90\sqrt{3}$  m
- c) 90 m                      d)  $60\sqrt{3}$  m
15. If  $\tan\theta = \frac{m}{n}$ , then  $\frac{m \sin \theta - n \cos \theta}{m \sin \theta + n \cos \theta} =$  [1]
- a)  $\frac{m^2 - n^2}{m^2 + n^2}$                       b)  $\frac{m^2 + n^2}{m^2 - n^2}$
- c) 1                      d)  $\frac{n^2 - m^2}{n^2 + m^2}$
16. The number of tangents that can be drawn from an external point to a circle is [1]
- a) 1                      b) 4
- c) 2                      d) 3
17. In a  $\triangle ABC$ ,  $\angle A = 90^\circ$ ,  $AB = 5$  cm and  $AC = 12$  cm. Also  $AD \perp BC$ , Then AD = [1]
- a)  $\frac{2\sqrt{15}}{13}$  cm                      b)  $\frac{60}{13}$  cm
- c)  $\frac{13}{40}$  cm                      d)  $\frac{13}{2}$  cm
18. **Assertion (A):** Graph of a quadratic polynomial is always U shaped upward or downward. [1]  
**Reason (R):** Curve of any quadratic polynomial is always symmetric about the fixed-line.
- a) Both A and R are true and R is the correct explanation of A.                      b) Both A and R are true but R is not the correct explanation of A.
- c) A is true but R is false.                      d) A is false but R is true.
19. By a reduction of Re.1 per kg in the price of sugar, Radha can buy one kg sugar more for Rs.56. The original price of 1 kg of sugar is [1]
- a) Rs.8                      b) Rs.7
- c) Rs.9                      d) Rs.6
20. **Assertion (A):** Two identical solid cubes of side 5 cm are joined end to end. The total surface area of the resulting cuboid is  $350 \text{ cm}^2$ . [1]  
**Reason (R):** Total surface area of a cuboid is  $2(lb + bh + hl)$
- a) Both A and R are true and R is the correct explanation of A.                      b) Both A and R are true but R is not the correct explanation of A.

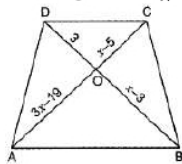


c) A is true but R is false.

d) A is false but R is true.

### Section B

21. Find the ratio in which point P(-1, y) lying on the line segment joining points A(-3, 10) and B(6, -8) divides it. Also find the value of y. [2]
22. Find the roots of the quadratic equation :  $2x^2 + x + 4 = 0$  by applying the quadratic formula: [2]
23. Find the largest four-digit number which when divided by 4, 7 and 13 leaves a remainder 3 in each case. [2]
24. In Fig.  $AB \parallel DC$ . Find the value of x. [2]



OR

If  $\triangle ABC$  and  $\triangle DEF$  are similar triangles such that  $AB = 3$  cm,  $BC = 2$  cm,  $CA = 2.5$  cm and  $EF = 4$  cm, calculate the perimeter of  $\triangle DEF$

25. Prove that:  $(\operatorname{cosec}^2 \theta - 1) \tan^2 \theta = 1$  [2]

OR

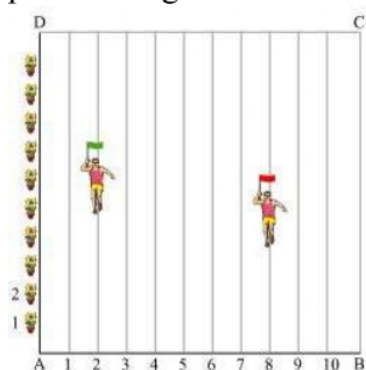
Using the formula,  $\cos A = \sqrt{\frac{1 + \cos 2A}{2}}$  find the value of  $\cos 30^\circ$ , it being given that  $\cos 60^\circ = \frac{1}{2}$

### Section C

26. In a  $\triangle ABC$ , D and E are points on the sides AB and AC respectively such that  $DE \parallel BC$ . If  $AD = 8x - 7$ ,  $DB = 5x - 3$ ,  $AE = 4x - 3$  and  $EC = (3x - 1)$ , find the value of x. [3]
27. Solve  $(x - 3)(x - 4) = \frac{34}{(33)^2}$  [3]
28. Find the HCF of the following polynomials: [3]  
 $2(x^4 - y^4)$ ,  $3(x^3 + 2x^2y - xy^2 - 2y^3)$
29. To conduct Sports Day activities, in your rectangular shaped school ground ABCD, lines have been drawn with chalk powder at a distance of 1m each. 100 flower pots have been placed at a distance of 1m from each other along AD, as shown in Fig. Niharika runs  $\frac{1}{4}$ th of the distance AD on the 2<sup>nd</sup> line and posts a green flag. Preet runs  $\frac{1}{5}$ th of the distance AD on the 8<sup>th</sup> line and posts a red flag. What is the distance between both the flags? If Rashmi has to post a blue flag exactly halfway between the line segment joining the two flags, where should she [3]



post her flag?



OR

Show that the points A(3, 5), B(6, 0), C(1, -3) and D(-2, 2) are the vertices of a square ABCD.

30. If the mean of the following frequency distribution is  $62.8$ , then find the missing frequency  $x$  : [3]

Class	0 – 20	20 – 40	40 – 60	60 – 80	80 – 100	100 – 120
Frequency	5	8	$x$	12	7	8

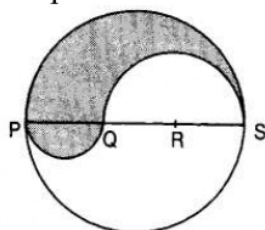
31. The angle of elevation of the top of a tower at a point on the level ground is  $30^\circ$ . After walking a distance of 100 m towards the foot of the tower along the horizontal line through the foot of the tower on the same level ground the angle of elevation to the top of the tower is  $60^\circ$ , find the height of the tower. [3]

OR

From a top of a building 100 m high the angle of depression of two objects are on the same side observed to be  $45^\circ$  and  $60^\circ$ . Find the distance between the objects.

### Section D

32. QR is the tangent to the circle whose centre is P. If QA  $\parallel$  RP and AB is the diameter, prove that RB is a tangent to the circle. [5]
33. PQRS is a diameter of a circle of radius 6 cm. The lengths PQ, QR and RS are equal. Semi-circles are drawn on PQ and QS as diameters as shown in Fig. Find the perimeter and area of the shaded region [5]

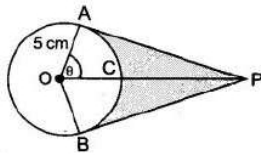


OR

An elastic belt is placed round the rim of a pulley of radius 5 cm. One point on the belt is pulled directly away from the centre O of the pulley until it is at P, 10 cm from O.

Find the length of the belt that is in contact with the rim of the pulley. Also, find the

shaded area.



34. Solve system of equations:

[5]

$$\frac{x}{7} + \frac{y}{3} = 5$$

$$\frac{x}{2} - \frac{y}{9} = 6$$

OR

Form the pair of linear equations in the problem, and find its solution (if it exists) by the elimination method:

A lending library has a fixed charge for the first three days and an additional charge for each day thereafter. Mona paid Rs.27 for a book kept for seven days, while Tanvy paid Rs.21 for the book she kept for five days. Find the fixed charge and the charge for each extra day.

35. All the red face cards are removed from a pack of 52 playing cards. A card is drawn at random from the remaining cards, after reshuffling them. Find the probability that the drawn card is:

[5]

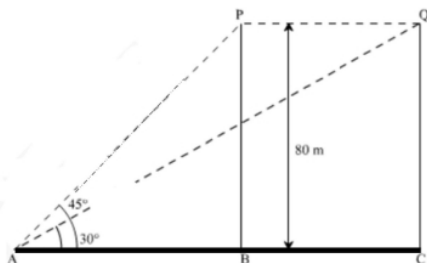
- of red colour
- a queen
- an ace
- a face card.

### Section E

36. Read the text carefully and answer the questions:

[4]

A bird is sitting on the top of a tree, which is 80m high. The angle of elevation of the bird, from a point on the ground is  $45^\circ$ . The bird flies away from the point of observation horizontally and remains at a constant height. After 2 seconds, the angle of elevation of the bird from the point of observation becomes  $30^\circ$ . Find the speed of flying of the bird.



- Find the distance between observer and the bottom of the tree?
- Find the speed of the bird?
- Find the distance between second position of bird and observer?

OR

Find the distance between initial position of bird and observer?

37. **Read the text carefully and answer the questions:**

[4]

Kamla and her husband were working in a factory in Seelampur, New Delhi. During the pandemic, they were asked to leave the job. As they have very limited resources to survive in a metro city, they decided to go back to their hometown in Himachal Pradesh. After a few months of struggle, they thought to grow roses in their fields and sell them to local vendors as roses have been always in demand. Their business started growing up and they hired many workers to manage their garden and do packaging of the flowers.



In their garden bed, there are 23 rose plants in the first row, 21 are in the 2<sup>nd</sup>, 19 in 3<sup>rd</sup> row and so on. There are 5 plants in the last row.

- (i) How many rows are there of rose plants?
- (ii) Also, find the total number of rose plants in the garden.

**OR**

If total number of plants are 80 in the garden, then find number of rows?

- (iii) How many plants are there in 6th row.

38. **Read the text carefully and answer the questions:**

[4]

A juice seller is serving his customers using cylindrical container with radius 20cm and height 50cm. He serves juice into a glass as shown in Fig. The inner diameter of the cylindrical glass is 5 cm, but the bottom of the glass had a hemispherical raised portion which reduced the capacity of the glass.



- (i) If the height of a glass was 10 cm, find the apparent capacity of the glass.
- (ii) Also, find its actual capacity. (Use  $\pi = 3.14$ )

**OR**

How many glasses he serves if the container is full?

- (iii) Find the capacity of the container in liter?



## SOLUTION

### Section A

1. (c)  $10x^2 - x - 3$

**Explanation:**  $\alpha + \beta = \left(\frac{3}{5} - \frac{1}{2}\right) = \frac{1}{10}$ ,  $\alpha\beta = \frac{3}{5} \times \left(\frac{-1}{2}\right) = \frac{-3}{10}$

Required polynomial is  $x^2 - \frac{1}{10}x - \frac{3}{10}$ , i.e.,  $10x^2 - x - 3$

2. (c)  $m = -1$

**Explanation:** Given:  $2x + 3y = 11$  ... (i)

$2x - 4y = -24$  ... (ii)

Subtracting eq. (ii) from eq. (i), we get

$7y = 35$

$\Rightarrow y = 5$

Putting the value of  $y$  in eq. (i), we get

$2x + 3 \times 5 = 11$

$\Rightarrow 2x = -4$

$\Rightarrow x = -2$

Now,  $y = mx + 3$

$\Rightarrow 5 = m \times (-2) + 3$

$\Rightarrow 2m = 3 - 5$

$m = -1$

3. (c)  $\frac{7}{9}$

**Explanation:** Let the fraction be  $\frac{x}{y}$ .

According to question

$\frac{x+2}{y+2} = \frac{9}{11}$

$\Rightarrow 11x + 22 = 9y + 18$

$\Rightarrow 11x - 9y = -4$  ... (i)

And  $\frac{x+3}{y+3} = \frac{5}{6}$

$\Rightarrow 6x + 18 = 5y + 15$

$\Rightarrow 6x - 5y = -3$  ... (ii)

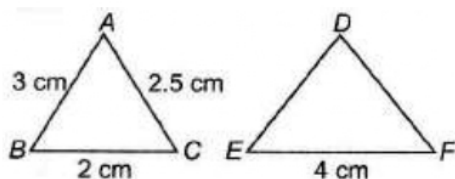
On solving eq. (i) and eq. (ii), we get

$x = 7, y = 9$

Therefore, the fraction is  $\frac{7}{9}$

4. (b) 15 cm

**Explanation:**



$\triangle DEF \sim \triangle ABC$

$AB = 3\text{ cm}, BC = 2\text{ cm}, CA = 2.5\text{ cm}, EF = 4\text{ cm}$

Since  $\triangle$ 's are similar, we have

$\frac{DE}{AB} = \frac{EF}{BC} = \frac{FD}{CA}$

$$\Rightarrow \frac{DE}{3} = \frac{4}{2} = \frac{FD}{2.5}$$

$$\text{Now } \frac{DE}{3} = \frac{4}{2}$$

$$\Rightarrow DE = \frac{3 \times 4}{2} = 6\text{cm}$$

$$\text{and } FD = \frac{4}{2} \Rightarrow FD = \frac{4 \times 2.5}{2} = 5\text{cm}$$

perimeter of  $\triangle DEF$

$$= 6 + 4 + 5 = 15\text{cm}$$

5. (a)  $\frac{1}{2}$

**Explanation:** Number of numbers between 2 and 6 on a dice =  $\{3, 4, 5\}$ , = 3

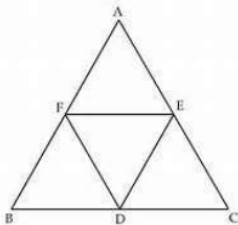
Number of possible outcomes = 3

Number of Total outcomes = 6

$$\therefore \text{Required Probability} = \frac{3}{6} = \frac{1}{2}$$

6. (d)  $\triangle FDE \sim \triangle CAB$

**Explanation:** Since  $\frac{AB}{DE} = \frac{BC}{FE} = \frac{CA}{FD}$ , then as sides are in proportion, then by SSS similarity criteria,  $\triangle FDE \sim \triangle CAB$



Also, FEDC is a parallelogram, then  $\angle F = \angle C$

And, AFDE is a parallelogram, then  $\angle D = \angle A$

And, BDEF is a parallelogram, then  $\angle E = \angle B$

Therefore, by AAA similarity criteria  $\triangle FDE \sim \triangle CAB$

7. (a) 11.2

**Explanation:** The first 10 composite numbers are 4, 6, 8, 9, 10, 12, 14, 15, 16, 18

$$\therefore \text{Mean} = \frac{\text{Sum of first 10 composite numbers}}{10}$$

$$= \frac{4+6+8+9+10+12+14+15+16+18}{10}$$

$$= \frac{112}{10}$$

$$= 11.2$$

8. (a) 23

**Explanation:** Given,  $\tan \theta + \cot \theta = 5$

Now squaring both sides,

$$(\tan \theta + \cot \theta)^2 = 5^2$$

$$\Rightarrow \tan^2 \theta + 2 \tan \theta \cot \theta + \cot^2 \theta = 25$$

$$\Rightarrow \tan^2 \theta + 2 \tan \theta \left( \frac{1}{\tan \theta} \right) + \cot^2 \theta = 25$$

$$\Rightarrow \tan^2 \theta + 2 + \cot^2 \theta = 25$$

$$\Rightarrow \tan^2 \theta + \cot^2 \theta = 25 - 2$$

$$\Rightarrow \tan^2 \theta + \cot^2 \theta = 23$$

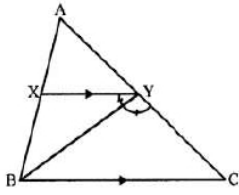
$$\therefore (\tan^2 \theta + \cot^2 \theta) = 23$$

9. (a)  $BC = CY$

**Explanation:** In  $\triangle ABC$ ,  $XY \parallel BC$



Also BY is the bisector  $\angle XYZ$



$$\angle XYB = \angle CYB \dots (i)$$

$$XY \parallel BC$$

$$\angle XYB = \angle YBC \text{ (Alternate angles are equal)} \dots (ii)$$

$$\angle CYB = \angle YBC$$

$$BC = CY$$

10. (c) 30 and 35

**Explanation:** Let one multiple of 5 be  $x$  then the next consecutive multiple will be  $(x + 5)$

According to question,

$$x(x + 5) = 1050$$

$$\Rightarrow x^2 + 5x - 1050 = 0$$

$$\Rightarrow x^2 + 35x - 30x - 1050 = 0$$

$$\Rightarrow x(x + 35) - 30(x + 35) = 0$$

$$\Rightarrow (x - 30)(x + 35) = 0$$

$$\Rightarrow x - 30 = 0 \text{ and } x + 35 = 0$$

$$\Rightarrow x = 30 \text{ and } x = -35$$

$x = -35$  is not possible therefore  $x = 30$

Then the other multiple of 5 is

$$= x + 5$$

$$= 30 + 5 = 35$$

Then the number are 30 and 35

11. (b)  $p^3 q^2$

**Explanation:** We know that LCM = product of the highest powers of all the prime factors of the numbers  $pq^2, p^3 q^2$

$$\text{LCM} = p^3 q^2$$

12. (b) 8

**Explanation:** Mode of a series = Its mean + 12

$$\text{Mean} = \text{mode} - 12$$

Also we know that

$$\text{Mode} = 3 \text{ median} - 2 \text{ Mean}$$

$$\Rightarrow \text{Mode} = 3 \text{ median} - 2(\text{mode} - 12)$$

$$\Rightarrow \text{Mode} = 3 \text{ median} - 2 \text{ mode} + 24$$

$$\Rightarrow \text{Mode} + 2 \text{ mode} - 3 \text{ median} = 24$$

$$\Rightarrow 3 \text{ mode} - 3 \text{ median} = 24$$

$$\Rightarrow 3(\text{mode} - \text{median}) = 24$$

$$\Rightarrow \text{Mode} - \text{median} = \frac{24}{3} = 8$$

13. (a) isosceles triangle

$$\text{Explanation: } AB^2 = (4 + 4)^2 + (0 - 0)^2 = 8^2 + 0^2 = 64 + 0 = 64$$

$$\Rightarrow AB = \sqrt{64} = 8 \text{ units}$$

$$BC^2 = (0-4)^2 + (3-0)^2 = (-4)^2 + 3^2 = 16 + 9 = 25$$

$$\Rightarrow BC = \sqrt{25} = 5 \text{ units.}$$

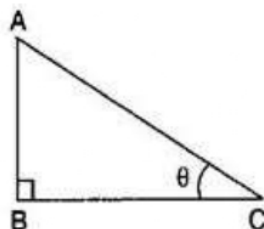
$$AC^2 = (0+4)^2 + (3-0)^2 = 4^2 + 3^2 = 16 + 9 = 25$$

$$\Rightarrow AC = \sqrt{25} = 5 \text{ units.}$$

$\therefore \triangle ABC$  is isosceles.

14. (b)  $90\sqrt{3}$  m

**Explanation:**



Let Height of the tower =  $AB = h$  meters,

Length of the shadow =  $BC = 90$  m

And angle of elevation  $\theta = 60^\circ$

$$\therefore \tan 60^\circ = \frac{AB}{BC}$$

$$\Rightarrow \sqrt{3} = \frac{h}{90}$$

$$\Rightarrow h = 90\sqrt{3} \text{ meters}$$

15. (a)  $\frac{m^2-n^2}{m^2+n^2}$

**Explanation:** Given:  $\tan \theta = \frac{m}{n}$

Dividing all the terms of  $\frac{m \sin \theta - n \cos \theta}{m \sin \theta + n \cos \theta}$  by  $\cos \theta$ ,

$$= \frac{m \tan \theta - n}{m \tan \theta + n}$$

$$= \frac{m \times \frac{m}{n} - n}{m \times \frac{m}{n} + n}$$

$$= \frac{m^2 - n^2}{m^2 + n^2}$$

$$= \frac{m^2 - n^2}{m^2 + n^2}$$

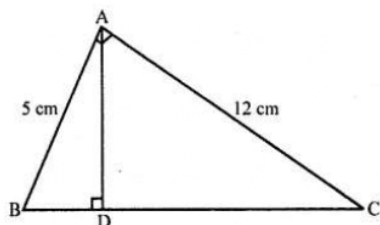
16. (c) 2

**Explanation:** Number of tangents drawn from an external point to a circle is 2.

17. (b)  $\frac{60}{13}$  cm

**Explanation:**

In  $\triangle ABC$   $\angle A = 90^\circ$ ,  $AB = 5$  cm,  $AC = 12$  cm



$AD \perp BC$

$$BC^2 = AB^2 + AC^2 \text{ (Pythagoras Theorem)}$$

$$= (5)^2 + (12)^2$$

$$= 25 + 144 = 169 = (13)^2$$

$$\therefore BC = 13 \text{ cm}$$

$$\text{Now area of } \triangle ABC = \frac{1}{2} AB \times AC$$

$$= \frac{1}{2} \times 5 \times 12 = 30 \text{ cm}^2$$

$$\text{and also area of } \triangle ABC = \frac{1}{2} BC \times AD$$

$$\Rightarrow 30 = \frac{1}{2} \times 13 \times AD$$

$$\Rightarrow AD = \frac{30 \times 2}{13} = \frac{60}{13} \text{ cm}$$

18. (a) Both A and R are true and R is the correct explanation of A.

**Explanation:** Both A and R are true and R is the correct explanation of A.

19. (a) Rs.8

**Explanation:** Let the original price of 1 kg sugar = Rs. x

$\therefore$  In Re. 1, the weight of sugar can be bought =  $\frac{1}{x}$  kg

$\therefore$  In Rs. 56, the weight of sugar can be bought =  $\frac{56}{x}$  kg

New price = Rs. (x - 1)

$\therefore$  In Rs. 56, the weight of sugar can be bought =  $\frac{56}{x-1}$  kg

According to question,  $\frac{56}{x-1} - \frac{56}{x} = 1$

$$\Rightarrow \frac{56x - 56(x-1)}{x(x-1)} = 1$$

$$\Rightarrow \frac{56}{x^2 - x} = 1$$

$$\Rightarrow x^2 - x - 56 = 0$$

$$\Rightarrow x^2 - 8x + 7x - 56 = 0$$

$$\Rightarrow x(x - 8) + 7(x - 8) = 0$$

$$\Rightarrow (x + 7)(x - 8) = 0$$

$$\Rightarrow x + 7 = 0 \text{ and } x - 8 = 0$$

$$\Rightarrow x = -7 \text{ and } x = 8 \text{ [} x = -7 \text{ is not possible]}$$

Therefore, the original price of 1 kg of sugar is Rs. 8

20. (d) A is false but R is true.

**Explanation:** A is false but R is true.

### Section B

21.  $\frac{K:1}{A(-3,10) \quad P(-1,y) \quad B(6,-8)}$

Let point P divides the line segment AB in the ratio K:1.

Applying section formula,

$$(-1, y) = \left( \frac{6k - 3}{k + 1}, -\frac{8k + 10}{k + 1} \right)$$

$$\therefore \frac{6k - 3}{k + 1} = -1$$

$$6k - 3 = -k - 1$$

$$7k = 2$$

$$k = \frac{2}{7}$$

$\therefore$  Required Ratio is 2:7

$$\text{Also, } y = -\frac{8k + 10}{k + 1}$$

$$= \frac{-8\left(\frac{2}{7}\right) + 10}{\frac{2}{7} + 1}$$

$$= \frac{-16 + 70}{2 + 7}$$

$$= \frac{54}{9}$$

$$\therefore y = 6$$

22. We have given that  $2x^2 + x + 4 = 0$

Comparing it with standard form of quadratic equation,

$$ax^2 + bx + c$$

we get,  $a = 2, b = 1, c = 4$

$$\begin{aligned} \text{The roots are given as } x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\ &= \frac{-1 \pm \sqrt{1 - 4(2)(4)}}{2 \times 2} = \frac{-1 \pm \sqrt{1 - 32}}{4} = \frac{-1 \pm \sqrt{-31}}{4} \end{aligned}$$

This is not possible, Hence the roots do not exist.

23. LCM of (4, 7, 13) = 364

Largest 4 digit number = 9999

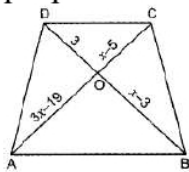
On dividing 9999 by 364 we get remainder as 171

Greatest number of 4 digits divisible by 4, 7 and 13 =  $(9999 - 171) = 9828$

Hence, required number =  $(9828 + 3) = 9831$

Therefore 9831 is the number.

24. We know that the diagonals of a trapezium divide each other proportionally. Therefore, we have,



$$\frac{AO}{OC} = \frac{BO}{OD} \dots (iii)$$

$$\Rightarrow \frac{3x-19}{x-5} = \frac{x-3}{3}$$

$$\Rightarrow 3(3x-19) = (x-5)(x-3)$$

$$\Rightarrow 9x - 57 = x^2 - 8x + 15$$

$$\Rightarrow x^2 - 17x + 72 = 0$$

$$\Rightarrow (x-8)(x-9) = 0$$

$$\Rightarrow x-8=0 \text{ or } x-9=0 \Rightarrow x=8 \text{ or } x=9$$

OR

Given:  $\triangle ABC$  and  $\triangle DEF$  are similar triangles such that  $AB = 3$  cm,  $BC = 2$  cm,  $CA = 2.5$  cm and  $EF = 4$  cm

To find: Perimeter of  $\triangle DEF$

We know that if two triangles are similar then their corresponding sides are proportional

$$\text{Hence, } \frac{AB}{DE} = \frac{BC}{EF} = \frac{CA}{FD}$$

Substituting the values, we get

$$\frac{AB}{BC} = \frac{DE}{EF}$$

$$\frac{3}{2} = \frac{DE}{4}$$

$$DE = 6 \text{ cm} \dots (i)$$

Similarly,

$$\frac{CA}{BC} = \frac{DF}{EF}$$

$$\frac{2.5}{2} = \frac{DF}{4}$$

$$DF = 5 \text{ cm} \dots (ii)$$

$$\text{Perimeter of } \triangle DEF = DE + EF + DF$$

$$= 6 + 4 + 5$$

$$= 15 \text{ cm}$$

25. We have,

$$\begin{aligned} \text{LHS} &= (\operatorname{cosec}^2 \theta - 1) \tan^2 \theta \\ &= (1 + \cot^2 \theta - 1) \tan^2 \theta \quad [\because \operatorname{cosec}^2 \theta = 1 + \cot^2 \theta] \\ &= \cot^2 \theta \cdot \tan^2 \theta \\ &= \frac{1}{\tan^2 \theta} \cdot \tan^2 \theta \quad [\because \cot \theta = \frac{1}{\tan \theta}] \\ &= 1 = \text{RHS} \end{aligned}$$

OR

$$\text{Given: } \cos A = \sqrt{\frac{1 + \cos 2A}{2}}, \dots (1)$$

$$\cos 60^\circ = \frac{1}{2}$$

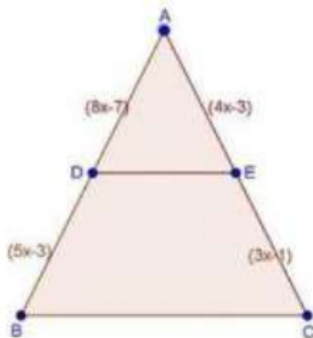
To find:  $\cos 30^\circ$

By putting  $A = 30^\circ$  in equation (1), we get the following:

$$\begin{aligned} \cos 30^\circ &= \sqrt{\frac{1 + \cos 60^\circ}{2}} \\ &= \sqrt{\frac{1 + (1/2)}{2}} \\ &= \sqrt{\frac{3}{4}} = \frac{\sqrt{3}}{2} \\ \therefore \cos 30^\circ &= \frac{\sqrt{3}}{2} \end{aligned}$$

### Section C

26. We have,



We are given that,  $DE \parallel BC$

Therefore, by thales theorem,

We have,

$$\begin{aligned} \frac{AD}{DB} &= \frac{AE}{EC} \\ \Rightarrow \frac{8x-7}{5x-3} &= \frac{4x-3}{3x-1} \\ \Rightarrow (8x-7)(3x-1) &= (4x-3)(5x-3) \\ \Rightarrow 24x^2 - 8x - 21x + 7 &= 20x^2 - 12x - 15x + 9 \\ \Rightarrow 24x^2 - 20x^2 - 29x + 27x + 7 - 9 &= 0 \\ \Rightarrow 4x^2 - 2x - 2 &= 0 \\ \Rightarrow 2[2x^2 - x - 1] &= 0 \\ \Rightarrow 2x^2 - x - 1 &= 0 \\ \Rightarrow 2x^2 - 2x + 1x - 1 &= 0 \\ \Rightarrow 2x(x-1) + 1(x-1) &= 0 \\ \Rightarrow (2x+1)(x-1) &= 0 \end{aligned}$$



$$\Rightarrow 2x + 1 = 0 \text{ or } x - 1 = 0$$

$$\Rightarrow x = -\frac{1}{2} \text{ or } x = 1$$

$x = -\frac{1}{2}$  is not possible.

$$\therefore x = 1.$$

27. Given,

$$(x - 3)(x - 4) = \frac{34}{33^2}$$

$$\Rightarrow x^2 - 4x - 3x + 12 = \frac{34}{33^2}$$

$$\Rightarrow x^2 - 7x + 12 - \frac{34}{33^2} = 0$$

$$\Rightarrow x^2 - 7x + \frac{13034}{33^2} = 0$$

$$\Rightarrow x^2 - 7x + \frac{98}{33} \times \frac{133}{33} = 0$$

$$\Rightarrow x^2 - \frac{231}{33}x + \frac{98}{33} \times \frac{133}{33} = 0$$

$$\Rightarrow x^2 - \left(\frac{98}{33} + \frac{133}{33}\right)x + \frac{98}{33} \times \frac{133}{33} = 0$$

$$\Rightarrow x^2 - \frac{98}{33}x - \frac{133}{33}x + \frac{98}{33} \times \frac{133}{33} = 0$$

$$\Rightarrow \left(x^2 - \frac{98}{33}x\right) - \left(\frac{133}{33}x - \frac{98}{33} \times \frac{133}{33}\right) = 0$$

$$\Rightarrow x\left(x - \frac{98}{33}\right) - \frac{133}{33}\left(x - \frac{98}{33}\right) = 0$$

$$\Rightarrow \left(x - \frac{98}{33}\right)\left(x - \frac{133}{33}\right) = 0 \Rightarrow x = \frac{98}{33} \text{ or } x = \frac{133}{33}$$

28. Let  $P(x) = 2(x^4 - y^4) = 2[(x^2)^2 - (y^2)^2]$

$$= 2(x^2 + y^2)(x^2 - y^2)$$

$$= 2(x^2 + y^2)(x + y)(x - y) \quad \text{Using Identity } a^2 - b^2 = (a + b)(a - b)$$

$$\text{and } Q(x) = 3(x^3 + 2x^2y - xy^2 - 2y^3)$$

$$= 3[x^2(x + 2y) - y^2(x + 2y)]$$

$$= 3(x + 2y)(x^2 - y^2)$$

$$= 3(x + 2y)(x + y)(x - y)$$

$$\therefore HCF = (x + y)(x - y) = x^2 - y^2 \quad \text{Using identity } a^2 - b^2 = (a + b)(a - b)$$

29. It can be observed that Niharika posted the green flag at  $\frac{1}{4}$ th of the distance AD i.e.,

$\frac{1}{4} \times 100 = 25m$  from the starting point of 2<sup>nd</sup> line. Therefore, the coordinates of this point G is (2, 25)

Similarly, Preet posted a red flag at  $\frac{1}{5}$ th of the distance AD i.e.,  $\frac{1}{5} \times 100 = 20m$  from

the starting point of 8<sup>th</sup> line. Therefore, the coordinates of this point R are (8, 20)

Now we have the positions of posts by Preet and Niharika

According to distance formula, the distance between points A( $x_1, y_1$ ) and B( $x_2, y_2$ )

is given by

$$D = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Distance between these flags by using distance formula,

$$D = \sqrt{(8 - 2)^2 + (25 - 20)^2}$$

$$= \sqrt{36 + 25}m$$

$$= \sqrt{61}m$$

The point at which Rashmi should post her blue flag is the mid-point of the line

joining these points. Let this point be A (X,Y)

Now by midpoint formula,

$$(X, Y) = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right)$$

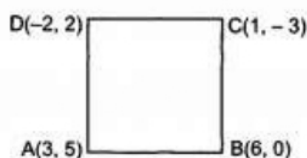
$$X = \left( \frac{2+8}{2} \right) = 5$$

$$Y = \left( \frac{25+20}{2} \right) = 22.5$$

Hence, A (X,Y) = (5, 22.5)

Therefore, Rashmi should post her blue flag at 22.5m on the 5<sup>th</sup> line.

OR



$$AB = \sqrt{(6-3)^2 + (0-5)^2}$$

$$= \sqrt{9+25} = \sqrt{34}$$

$$BC = \sqrt{(6-1)^2 + (0+3)^2}$$

$$= \sqrt{25+9} = \sqrt{34}$$

$$CD = \sqrt{(1+2)^2 + (-3-2)^2}$$

$$= \sqrt{9+25} = \sqrt{34}$$

$$DA = \sqrt{(-2-3)^2 + (2-5)^2}$$

$$= \sqrt{25+9} = \sqrt{34}$$

$$AC = \sqrt{(1-3)^2 + (-3-5)^2}$$

$$= \sqrt{4+64} = \sqrt{68}$$

$$BD = \sqrt{(6+2)^2 + (0-2)^2}$$

$$= \sqrt{64+4} = \sqrt{68}$$

$$AB = BC = CD = DA = \sqrt{34}$$

$$\text{Diagonal AC} = \text{diagonal BD} = \sqrt{68}$$

Hence A, B, C and D are vertices of a square.

30. We have

Class interval	Frequency ( $f_i$ )	Class mark ( $x_i$ )	$f_i x_i$
0 - 20	5	10	50
20-40	8	30	240
40-60	x	50	50x
60-80	12	70	840
80-100	7	90	630
100-120	8	110	880
Total	$\Sigma f_i = 40 + x$		$\Sigma f_i x_i = 2640 + 50x$

Here,  $\Sigma f_i x_i = 2640 + 50x$ ,  $\Sigma f_i = 40 + x$ ,  $\bar{X} = 62.8$

$$\therefore \text{Mean}(\bar{X}) = \frac{\Sigma f_i x_i}{\Sigma f_i}$$

$$\Rightarrow 62.8 = \frac{2640+50x}{40+x}$$

$$\Rightarrow 2512 + 62.8x = 2640 + 50x$$

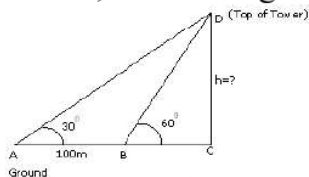
$$\Rightarrow 62.8x - 50x = 2640 - 2512$$

$$\Rightarrow 12.8x = 128$$

$$\therefore x = \frac{128}{12.8} = 10$$

Hence, the missing frequency is 10

31.



$$\text{In } \triangle BCD, \frac{h}{x} = \tan 60^\circ = \sqrt{3} \text{ (BC=x)}$$

$$h = \sqrt{3}x \dots\dots\dots(i)$$

$$\text{In } \triangle ACD, \frac{h}{100+x} = \tan 30^\circ = \frac{1}{\sqrt{3}}$$

$$\Rightarrow h\sqrt{3} = 100 + x$$

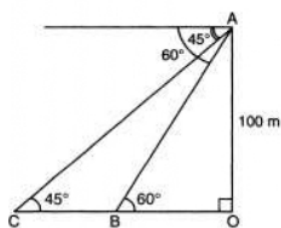
$$\Rightarrow h\sqrt{3} = 100 + \frac{h}{\sqrt{3}}$$

$$\Rightarrow h \left[ \sqrt{3} - \frac{1}{\sqrt{3}} \right] = 100$$

$$\Rightarrow h \left[ \frac{3-1}{\sqrt{3}} \right] = 100$$

$$\Rightarrow h = \frac{100\sqrt{3}}{2} = 50\sqrt{3} = 50 \times 1.732 = 86.6\text{m}$$

OR



In the given figure,

$$\angle ACO = \angle CAX = 45^\circ$$

$$\text{and } \angle ABO = \angle XAB = 60^\circ$$

Let A be a point and B, C be two objects.

$$\text{In } \triangle AOC, \frac{AO}{CO} = \tan 45^\circ$$

$$\Rightarrow \frac{100}{CO} = 1$$

$$\Rightarrow CO = 100\text{m}$$

$$\text{Also in } \triangle ABO, \frac{AO}{OB} = \tan 60^\circ$$

$$\Rightarrow \frac{100}{OB} = \sqrt{3}$$

$$\Rightarrow OB = \frac{100}{\sqrt{3}}$$

$$\therefore BC = CO - OB = 100 - \frac{100}{\sqrt{3}}$$

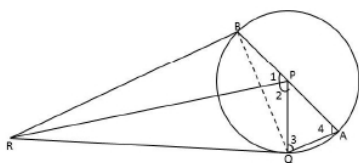
$$= 100 \left( 1 - \frac{1}{\sqrt{3}} \right) \text{m}$$

$$100 \frac{(\sqrt{3}-1)}{\sqrt{3}} = 100 \frac{(\sqrt{3}-1)}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$$

$$= \frac{100(3-\sqrt{3})}{3} \text{m}$$

Section D

32.



**Given:** A circle with centre P, AB is the diameter.

QA || RP, where RQ is the tangent to the circle.

**To prove:** RB is tangent to the circle i.e.  $\angle RBP = 90^\circ$ .

**Construction:** Join BQ and PQ.

**Proof:** RQ is tangent to the circle and PQ is the radius at point of contact Q.

$\therefore PQ \perp RQ$  (radius of a circle is perpendicular to the tangent at point of contact)

$\Rightarrow \angle PQR = 90^\circ \dots (1)$

QA || RP and PQ is the transversal.

$\Rightarrow \angle 2 = \angle 3 \dots (2)$  (Alternate interior angles)

But, PQ = PA (radii of the circle)

$\therefore$  In  $\triangle PQA$ ,  $\angle 3 = \angle 4 \dots (3)$  (Angles opposite to equal sides are equal)

From (2) and (3)  $\Rightarrow \angle 2 = \angle 3 = \angle 4$

$\angle BPQ$  and  $\angle BAQ$  are the angles made by the arc BQ at the centre P and on the remaining part of the circle respectively.

$\therefore \angle BPQ = 2 \angle BAQ$

i.e.,  $\angle 1 + \angle 2 = 2 \angle 4$

$\Rightarrow \angle 1 + \angle 2 = \angle 4 + \angle 4$

$\Rightarrow \angle 1 = \angle 4$  (as  $\angle 2 = \angle 4$ )

So,  $\angle 1 = \angle 2 = \angle 3 = \angle 4$

$\Rightarrow \angle 1 = \angle 2$

In  $\triangle BPR$  and  $\triangle RPQ$ ,

BP = PQ (radii of the circle)

$\angle 1 = \angle 2$  (proved)

RP = RP (common)

$\therefore \triangle BPR \cong \triangle RPQ$  (SAS congruency)

$\Rightarrow \angle PBR = \angle PQR$  (corresponding angles)

But  $\angle PQR = 90^\circ$  from equation (1)

i.e.,  $PB \perp BR$

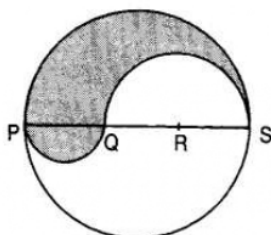
Therefore, RB is a tangent to the circle at point B.

33. PS = Diameter of a circle of radius 6 cm = 12 cm

$\therefore PQ = QR = RS = \frac{12}{3} = 4$  cm, QS = QR + RS = (4 + 4) cm = 8 cm

Let P be the perimeter and A be the area of the shaded region.

P = Arc of semi-circle of radius 6 cm + Arc of semi-circle of radius 4 cm + Arc of semi-circle of radius 2 cm



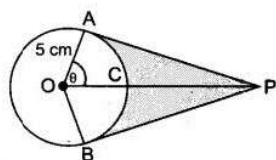
$$\Rightarrow P = (\pi \times 6 + \pi \times 4 + \pi \times 2)\text{cm} = 12\pi\text{cm}$$

and, A = Area of semi-circle with PS as diameter + Area of semi-circle with PQ as diameter - Area of semi-circle with QS as diameter.

$$\Rightarrow A = \frac{1}{2} \times \frac{22}{7} \times (6)^2 + \frac{1}{2} \times \frac{22}{7} \times 2^2 - \frac{1}{2} \times \frac{22}{7} \times (4)^2$$

$$\Rightarrow A = \frac{1}{2} \times \frac{22}{7} (6^2 + 2^2 - 4^2) = \frac{1}{2} \times \frac{22}{7} \times 24 = \frac{264}{7}\text{cm}^2 = 37.71\text{ cm}^2$$

OR



$$\cos \theta = \frac{1}{2} \text{ or, } \theta = 60^\circ$$

$$\text{Reflex } \angle AOB = 120^\circ$$

$$\therefore \text{ADB} = \frac{2 \times 3.14 \times 5 \times 240}{360} = 20.93\text{ cm}$$

Hence length of elastic in contact = 20.93 cm

$$\text{Now, AP} = 5\sqrt{3}\text{cm}$$

$$a(\triangle OAP) = \frac{1}{2} \times \text{base} \times \text{height} = \frac{1}{2} \times 5 \times 5\sqrt{3} = \frac{25\sqrt{3}}{2}$$

$$\text{Area}(\triangle OAP + \triangle OBP) = 2 \times \frac{25\sqrt{3}}{2} = 25\sqrt{3} = 43.25\text{ cm}^2$$

$$\text{Area of sector OACB} = \frac{\theta}{360} \times \pi r^2$$

$$= \frac{25 \times 3.14 \times 120}{360} = 26.16\text{ cm}^2$$

$$\text{Shaded Area} = 43.25 - 26.16 = 17.09\text{ cm}^2$$

34. The given system of equations is

$$\frac{x}{7} + \frac{y}{3} = 5 \dots\dots\dots(i)$$

$$\frac{x}{2} - \frac{y}{9} = 6 \dots\dots\dots(ii)$$

From (i), we get

$$3x + 7y = 5(21)$$

$$\Rightarrow 3x + 7y = 105$$

$$\Rightarrow 3x = 105 - 7y$$

$$x = \frac{105-7y}{3} \dots\dots\dots(iii)$$

From (ii), we get

$$\frac{9x-2y}{18} = 6$$

$$\Rightarrow 9x - 2y = 18(6)$$

$$\Rightarrow 9x - 2y = 108 \dots(iv)$$

Substituting (iii) in (iv), we get

$$9\left(\frac{105-7y}{3}\right) - 2y = 108$$

$$\Rightarrow \frac{945-63y}{3} - 2y = 108$$

$$\Rightarrow 945 - 63y - 6y = 108 \times 3$$

$$\Rightarrow 945 - 69y = 324$$

$$\Rightarrow 945 - 324 = 69y$$

$$\Rightarrow 69y = 621$$

$$\Rightarrow y = \frac{621}{69} = 9$$

Putting y = 9 in (iii), we get



$$\begin{aligned}
 x &= \frac{105 - 7 \times 9}{3} \\
 &= \frac{105 - 63}{3} \\
 \Rightarrow x &= \frac{42}{3} \\
 \therefore x &= 14
 \end{aligned}$$

Hence, the solution of the given system of equations is  $x = 14$ ,  $y = 9$ .

OR

Suppose the fixed charge be Rs.  $x$  and the extra charge per day be Rs.  $y$ .  
According to the question, Mona paid Rs 27 for a book kept for 7 days,

$$\Rightarrow x + 4y = 27 \dots\dots(i)$$

Tanvy paid Rs.21 for a book kept for 5 days,

$$\Rightarrow x + 2y = 21 \dots\dots(ii)$$

Subtracting (ii) from (i),

$$\Rightarrow 2y = 6$$

$$\Rightarrow y = 3$$

Substituting  $y = 3$  in (ii), we get  $x = 15$

The fixed charge is Rs. 15 and the charge per day is Rs 3.

35. No. of cards removed = 3 face cards of heart + 3 face cards of diamond = 6

$$\text{Remaining cards} = 52 - 6 = 46$$

So total No. of events are  $n = 46$

(i) No. of red card left =  $13 - 6 = 7$  so  $m = 7$

$$\text{so } P(E) = \frac{7}{46}$$

(ii) No. of queen left =  $4 - 2$  queens of heart and diamond = 2

So  $m = 2$

$$P(E) = \frac{2}{46} = \frac{1}{23}$$

(iii) Total No. of aces = 4 so  $m = 4$

$$P(E) = \frac{4}{46} = \frac{2}{23}$$

(iv) No. of face cards left =  $12 - \text{total face cards removed} = 12 - 6 = 6$

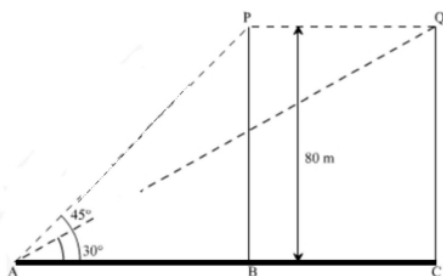
So  $m = 6$

$$\text{Hence } P(E) = \frac{6}{46} = \frac{3}{23}$$

### Section E

36. Read the text carefully and answer the questions:

A bird is sitting on the top of a tree, which is 80m high. The angle of elevation of the bird, from a point on the ground is  $45^\circ$ . The bird flies away from the point of observation horizontally and remains at a constant height. After 2 seconds, the angle of elevation of the bird from the point of observation becomes  $30^\circ$ . Find the speed of flying of the bird.



- (i) Given height of tree = 80m, P is the initial position of bird and Q is position of bird after 2 sec the distance between observer and the bottom of the tree

In  $\triangle ABP$

$$\tan 45^\circ = \frac{BP}{AB}$$

$$\Rightarrow 1 = \frac{80}{AB}$$

$$\Rightarrow AB = 80 \text{ m}$$

- (ii) The speed of the bird

In  $\triangle AQC$

$$\tan 30^\circ = \frac{QC}{AC}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{80}{AC}$$

$$\Rightarrow AC = 80\sqrt{3} \text{ m}$$

$$AC - AB = BC$$

$$\Rightarrow BC = 80\sqrt{3} - 80 = 80(\sqrt{3} - 1) \text{ m}$$

$$\text{Speed of bird} = \frac{\text{Distance}}{\text{Time}}$$

$$\Rightarrow \frac{BC}{2} = \frac{80(\sqrt{3}-1)}{2} = 40(\sqrt{3} - 1)$$

$$\Rightarrow \text{Speed of the bird} = 29.28 \text{ m/sec}$$

- (iii) The distance between second position of bird and observer.

In  $\triangle AQC$

$$\sin 30^\circ = \frac{QC}{AQ}$$

$$\Rightarrow \frac{1}{2} = \frac{80}{AQ}$$

$$\Rightarrow AQ = 160 \text{ m}$$

OR

The distance between initial position of bird and observer.

In  $\triangle ABP$

$$\sin 45^\circ = \frac{BP}{AP}$$

$$\Rightarrow \frac{1}{\sqrt{2}} = \frac{80}{AP}$$

$$\Rightarrow AP = 80\sqrt{2} \text{ m}$$

**37. Read the text carefully and answer the questions:**

Kamla and her husband were working in a factory in Seelampur, New Delhi. During the pandemic, they were asked to leave the job. As they have very limited resources to survive in a metro city, they decided to go back to their hometown in Himachal Pradesh. After a few months of struggle, they thought to grow roses in their fields and sell them to local vendors as roses have been always in demand. Their business started growing up and they hired many workers to manage their garden and do packaging of the flowers.



In their garden bed, there are 23 rose plants in the first row, 21 are in the 2<sup>nd</sup>, 19 in 3<sup>rd</sup> row and so on. There are 5 plants in the last row.

- (i) The number of rose plants in the 1<sup>st</sup>, 2<sup>nd</sup>, .... are 23, 21, 19, ... 5

$$a = 23, d = 21 - 23 = -2, a_n = 5$$

$$\therefore a_n = a + (n - 1)d$$

$$\text{or, } 5 = 23 + (n - 1)(-2)$$

$$\text{or, } 5 = 23 - 2n + 2$$

$$\text{or, } 5 = 25 - 2n$$

$$\text{or, } 2n = 20$$

$$\text{or, } n = 10$$

- (ii) Total number of rose plants in the flower bed,

$$S_n = \frac{n}{2}[2a + (n - 1)d]$$

$$S_{10} = \frac{10}{2}[2(23) + (10 - 1)(-2)]$$

$$S_{10} = 5[46 - 20 + 2]$$

$$S_{10} = 5(46 - 18)$$

$$S_{10} = 5(28)$$

$$S_{10} = 140$$

OR

$$S_n = 80$$

$$S_n = \frac{n}{2}[2a + (n - 1)d]$$

$$\Rightarrow 80 = \frac{n}{2}[2 \times 23 + (n - 1) \times -2]$$

$$\Rightarrow 80 = 23n - n^2 + n$$

$$\Rightarrow n^2 - 24n + 80 = 0$$

$$\Rightarrow (n - 4)(n - 20) = 0$$

$$\Rightarrow n = 4 \text{ or } n = 20$$

$$n = 20 \text{ not possible}$$

$$a_{20} = 23 + 19 \times (-2) = -15$$

Number of plants cannot be negative.

$$n = 4$$

- (iii)  $a_n = a + (n - 1)d$

$$\Rightarrow a_6 = 23 + 5 \times (-2)$$

$$\Rightarrow a_6 = 13$$

### 38. Read the text carefully and answer the questions:

A juice seller is serving his customers using cylindrical container with radius 20cm and height 50cm. He serves juice into a glass as shown in Fig. The inner diameter of the cylindrical glass is 5 cm, but the bottom of the glass had a hemispherical raised

portion which reduced the capacity of the glass.



- (i) We have, Inner diameter of the glass,  $d = 5$  cm, Height of the glass = 10 cm

The apparent capacity of the glass = Volume of cylinder

$$= \pi r^2 h$$

$$= 3.14 \times \left(\frac{5}{2}\right)^2 \times 10$$

$$= 3.14 \times \frac{25}{4} \times 10 = 196.25 \text{ cm}^3$$

- (ii) We have, Inner diameter of the glass,  $d = 5$  cm, Height of the glass = 10 cm

The actual capacity of glass = Apparent capacity of glass - Volume of hemispherical part of the glass

$$\text{The volume of hemispherical part} = \frac{2}{3} \pi r^2 h = \frac{2}{3} \times 3.14 \times \left(\frac{5}{2}\right)^3 = 32.71 \text{ cm}^3$$

$$\text{Actual capacity of glass} = 196.25 - 32.71 = 163.54 \text{ cm}^3$$

OR

We have, Inner diameter of the glass,  $d = 5$  cm, Height of the glass = 10 cm

$$\text{Number of glasses} = \frac{\text{Volume of container}}{\text{Actual volume of one glass}}$$

$$\Rightarrow \text{Number of glasses} = \frac{20 \times 3.14 \times 20 \times 50}{3.14 \times \frac{2\pi}{4} \times 10 - \frac{2}{3} \times 3.14 \times \frac{125}{8}}$$

$$\Rightarrow \text{Number of glasses} = \frac{20000}{\frac{250}{4} - \frac{125}{12}} = \frac{20000 \times 12}{750 - 125} = \frac{240000}{625} = 384$$

$$\Rightarrow \text{Number of glasses} = 384$$

- (iii) We have, inner diameter of the glass,  $d = 5$  cm, height of the glass = 10 cm

$$\text{Volume of container} = V = \pi r^2 h$$

$$\Rightarrow V = 3.14 \times 20 \times 20 \times 50 = 62800 \text{ cm}^3$$

$$\Rightarrow V = 62.8 \text{ litre}$$